Lassonde School of Engineering

Dept. of EECS

Professor G. Tourlakis

EECS 1028 M. Problem Set No1

Posted: Jan. 16, 2022

Due: Jan. 31, 2022; by 4:35pm, in eClass.

Q: How do I submit?

A:

- (1) Submission must be a SINGLE *standalone* file to <u>eClass</u>. Submission by email is not accepted.
- (2) Accepted File Types: PNG, JPEG, PDF, RTF, MS WORD, OPEN OFFICE, ZIP
- (3) Deadline is strict, electronically limited.
- (4) MAXIMUM file size = 10MB



It is worth remembering (from the course outline):

The homework **must** be each individual's <u>own work</u>. While consultations with the <u>instructor</u>, <u>tutor</u>, and <u>among students</u>, are part of the <u>learning process</u> and are encouraged, **nevertheless**, at the end of all this consultation each student will have to produce an <u>individual report</u> rather than a *copy* (full or partial) of somebody else's report.

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The concept of "late assignments" does not exist in this course, as you recall.



1. True or False and Why.

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- (a) $(2 \text{ MARKS}) \{\{1\}, \{42\}\} = \{1, 42\}$
- (b) $(2 \text{ MARKS}) \bigcup \{\{1\}, \{42\}\} = \{1, 42\}$
- (c) $(2 \text{ MARKS}) \bigcup \{1, \{1, 42\}\} = \text{is What? Why?}$
- (d) (2 MARKS) $\{\emptyset\} = \emptyset$ (you do not have to involve stages! But OK if you do)
- (e) (2 MARKS) $\emptyset \in \{\emptyset\}$
- **2.** (3 MARKS) Is there a set A that satisfies $A = \{A\}$? If yes, exhibit one such. If not, **Why** not exactly?
- **3.** (4 MARKS) Prove that if A is a set then so is $\{A\}$ but do NOT use an argument that involves stages *explicitly*.
- **4.** (5 MARKS) Prove that, for any sets A and B, it is true that $A \subseteq B$ iff $A \cap B = A$.

Hint. There are two directions! lhs of iff implies rhs, and rhs of iff implies lhs.

- **5.** (4 MARKS) What is $\bigcup F$, where $F = \emptyset$? Prove the correctness of your *answer* / *computation*.
- **6.** Use notation by explicitly listing **all the members** of each rhs {???} to complete the following incomplete equalities:
 - (a) $(2 \text{ MARKS}) 2^{\emptyset} = \{???\}$
 - (b) $(2 \text{ MARKS}) \ 2^{\{\emptyset\}} = \{???\}$
 - (c) $(2 \text{ MARKS}) \ 2^{\{1,2\}} = \{???\}$
 - (d) (2 MARKS) $2^{\{a,b,3\}} = \{???\}$

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