This page <u>must</u> be submitted as the <u>first</u> page of your MidTerm-paper answer pages.

York University Department of Electrical Engineering and Computer Science Lassonde School of Engineering

EECS 1028M. <u>MID TERM</u>, March 9, 2022; 13:30(pm) – 14:30(pm) Professor George Tourlakis

By putting my name and student ID on this MID TERM page, I attest to the fact that my answers included here and submitted by Moodle are my own work, and that I have acted with integrity, abiding by the *Senate Policy on Academic Honesty* that the instructor discussed at the beginning of the course and *linked the full Policy to the Course Outline*.

Student NAME (Clearly):_____

Student NUMBER (Clearly):

DATE (Cearly):____

README FIRST! INSTRUCTIONS:

- 1. Please read ALL these instructions carefully before you start writing.
- 2. This is a TIME-LIMITED ON LINE *MID TERM*. You have 60 MIN to answer the MidTerm questions. <u>ABSOLUTELY</u> last opportunity to <u>upload</u> is <u>BY 14:45 (pm)</u> —that is 15min MAX extra time is allocated to <u>upload</u> your answers to *eClass*.
- **3.** Only ONE file —size <u>no more than</u> 10MB can be uploaded per student.
- **4.** If you submit photographed copy **it still must be ONE file that you submit**. Either ZIP the PNG or JPEG images **OR** import them in MS Word and submit *ONE* Word *file* with the photos attached.
- 5. Using the time allotted for the <u>uploading mechanisms</u> (15 min) for the MidTerm-answering part is at your own *risk*. MidTerm not uploaded <u>on time</u> = MidTerm <u>not</u> written.
- 6. Please write your answers by hand —see also 3. above— as you normally do for assignments or use a word processor that can convert to PDF. MS Word is acceptable to upload <u>as is</u> (without conversion to PDF).

Question	MAX POINTS	MARK
1	7	
2	5	
3	5	
4	6	
TOTAL	23	

Question 1. (a) (2 MARKS) Define *Correctly* " \mathbb{P} is an order".

- (b) (2 MARKS) State *Correctly* **Principle** 0 and **Principle** 1 of set formation by stages.
- (c) (3 MARKS) Using said principles (state **exactly** which one was used **where**) prove that for any sets *A*, *B* the following statement is **false**.

 $A\in B\in A$

Question 2. (5 Marks) Prove that if $A \cup B = A$ is true, then $A \cap B = B$ is also true, AND CONVERSELY.

Caution. There are two directions to prove.

Question 3. (5 Marks) If \mathbb{F} is a function and dom (\mathbb{F}) is a set, then \mathbb{F} is a set. *Hint*. Prove <u>first</u> that ran (\mathbb{F}) is a set.

Question 4. Consider the functions $f : A \to B$, $g : B \to A$ and $h : B \to A$ such that if $gf = \mathbf{1}_A$ and $fh = \mathbf{1}_B$.

Prove

- (a) (3 MARKS) f is a 1-1 correspondence $A \sim B$.
- (b) (3 MARKS) $f\mathbf{1}_A = f$ and $\mathbf{1}_B f = f$.