

## **Deferred Final Examination — May 13, 2022**

Duration: 120 minutes

No Aids Allowed

Total marks: 75

**Name:**

**Student Number:**

1)	/5
2)	/5
3)	/5
4)	/5
5)	/5
6)	/15
7)	/10
8)	/10
9)	/15
Total	/75

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3. [5 points] A popular fragment of first-order logic is *Horn clauses*. What is a Horn clause? What are the expressive limitations of Horn clauses knowledge bases? That is, what kind of knowledge cannot be expressed using Horn clauses?

4. [5 points] Consider an undiscounted MDP with states  $s_0, s_1, s_2, s_3$ , and  $s_4$ , where  $s_0$  is the starting state, and  $s_3$  and  $s_4$  are terminal states. The reward in  $s_4$  is  $+1$ , in  $s_3$  it is  $-1$ , and in all other states it is  $0$ . Action  $a$  is only possible in  $s_0$  and leads to  $s_1$  with probability  $0.6$  and to  $s_2$  with probability  $0.4$ . Action  $b$  is possible in  $s_1$  and leads to  $s_3$  with probability  $0.8$  and to  $s_4$  with probability  $0.2$ ; it is also possible in  $s_2$  and leads to  $s_3$  with probability  $0.1$  and to  $s_4$  with probability  $0.9$ . Action  $c$  is possible in  $s_1$  and leads to  $s_3$  with probability  $0.3$  and to  $s_4$  with probability  $0.7$ ; it is also possible in  $s_2$  and leads to  $s_3$  with probability  $0.6$  and to  $s_4$  with probability  $0.4$ . (No actions are possible in the terminal states.)

What is the expected value of the policy  $\pi$  where  $\pi(s_0) = a$ ,  $\pi(s_1) = c$ , and  $\pi(s_2) = b$ ? Show how you compute this value.

5. [5 points] Show using logical interpretations that  $\exists x.(P(x) \vee Q(x))$  does *not* logically entail  $\exists x.P(x)$ . Give a detailed argument.

6. [15 points] Assume the following facts:

(1) John likes all desserts.

(2) Chocolate cake is a dessert.

(3) Apple pie is a dessert.

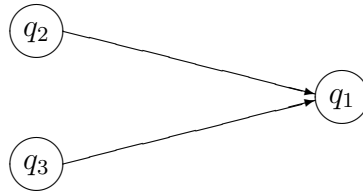
(4) Mary does not like chocolate cake.

(a) For each fact, give its translation in first-order logic.

(b) Convert all of the above facts into clausal form.

- (c) Use resolution to answer the question “What dessert does John like that Mary does not like?”. Indicate clearly which clauses are resolved and what substitutions are used.

7. [10 points] Suppose that we have the following belief network (or Bayes net):



- (a) Give an example of an independence assumption that is implicit in this network (write it formally).
- (b) What are the 6 conditional probabilities that need to be specified to fully determine the joint probability distribution?
- (c) Express  $Pr(q_1|q_3)$  in terms of the 6 conditional probabilities given in your answer to the previous question.

8. [10 points] Consider the following STRIPS actions:

Action Name	Preconditions	Add Effects	Delete Effects
A	p	r	-
B	-	p	-
C	o	-	o
D	p	q	r

Suppose that the start state is  $S_0 = \{o\}$  and the goal is  $G = \{p, q, r, o\}$ .

- (a) Which actions are applicable in the start state  $S_0$ ? What is the new state for each of the applicable actions?
- (b) Suppose we want to do backward/regression planning. Which actions are consistent with the goal  $G$ ? What is the regressed goal for all the consistent actions?
- (c) Give a sequence of actions that achieves the goal  $G$  when executed in the starting state  $S_0$ .



9. [15 points] Consider the following dynamic domain, to be specified in the situation calculus. Suppose that we have a fluent  $IsOpen(x, s)$  that is true if and only if door  $x$  is open in situation  $s$  and another fluent  $IsLocked(x, s)$  that is true if and only if door  $x$  is locked in situation  $s$ . Suppose also that we have an action  $open(x)$  whose only effect is to open a closed (i.e., not open) door  $x$  provided that  $x$  is not locked, as well as an action  $close(x)$  whose only effect is to close an open door  $x$ .  $open(x)$  can be executed whenever door  $x$  is open and  $close(x)$  can be executed whenever door  $x$  is closed. Performing  $open(x)$  when door  $x$  is locked has no effect. Finally, assume that these are the only actions that affect the fluent  $IsOpen$ .
- a) Write effect axioms for the actions  $open$  and  $close$ ; your axioms should capture all the effects of the actions.
- b) Write frame axiom(s) for the action  $open$  and the fluent  $IsOpen$ ; your axioms should handle all cases where the fluent does not change when  $open$  is performed.
- c) Write a successor state axiom for the fluent  $IsOpen(x, s)$ .

- d)** Suppose that the that doors  $D1$  and  $D2$  are both closed (i.e., not open) and unlocked initially. Write a sentence in the situation calculus that represents the *planning task* for the goal of having both  $D1$  and  $D2$  open.
- e)** Write a ground situation term that represents a plan that is achieves the goal of having both  $D1$  and  $D2$  open in an initial situation as described above.
- f)** This domain cannot be represented directly in STRIPS. Briefly explain why. Also describe how you could change the language to allow the domain to be represented in STRIPS.

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